HEAT CAPACITY MEASUREMENTS ON Sn₂S₃ AND THE

THERMODYNAMIC FUNCTIONS OF THE TIN SULFIDES

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ABSTRACT

The heat capacity of $Sn₂S₃$ was measured in the temperature range $110-610$ K, em**ploying a computer-interfaced differential scanning calorimeter. The sum of the known** heat capacities of SnS and SnS₂ agreed with the measured heat capacity of Sn₂S₃ from 110 to 610 K. Structural and bonding similarities between Sn₂S₃, SnS and SnS₂ justify the extrapolation of the heat capacity of $Sn₂S₃$ from 110 to 0 K, using the sum of the heat capacities of SnS and SnS₂. With the measured and extrapolated heat capacity data of Sn₂S₃, the absolute entropy, enthalpy and free enthalpy have been evaluated (S₂₉₈ = 163.6 ± 6 J K⁻¹ mole⁻¹, $H_{298}^{\prime} - H_0^{\prime} = 23.7 \pm 1$ kJ mole⁻¹ and $G_{298}^{\prime} - H_0^{\prime} = -25.1 \pm 2$ kJ mole⁻¹) for $Sn₂S₃$.

INTRODUCTION

Studies of the vaporization of SnS [la], Sn& [lb], and SnS, [lb] and characterization of the chemical vapor transport and crystal growth properties of SnS₂ [2] require the knowledge of thermodynamic properties of all **compounds involved as a function of temperature. The heat capacities of** SnS and SnS₂ have been determined at both low [3] and high [4] temperatures, but the corresponding data for $Sn₂S₃$ were not available. This paper presents measurements of the heat capacity of $Sn₂S₃$ in the temperature **range 110.--610 K. These data are compared to the known heat capacities of** SnS and SnS₂ [3,4]. Based on this comparison, the heat capacity of $Sn₂S₃$ **is extrapolated to 0 K using empirical equations_ Tabulations of the thermodynamic parameters for all tin sulfides are presented.**

EXPERIMENTAL PROCEDURES

Heat capacity instrumentation

A differential scanning calorimeter (Perkin-Elmer DSC-2) was used for the thermal analysis of the Sn₂S₃ samples. An enclosed, air-cooled refrigeration **unit (Perkin-Elmer Intracooler II) was attached to the DSC allowing heat capacity measurements to temperatures of 210 K. Using the liquid nitrogen accessory (Perkin-Elmer 319-0027) the lower temperature limit of the heat capacity measurements was extended to 100 K. Continuous transformation**

of the output amplitudes into digital form was accomplished through the use of an analog/digital converter (Perkin-Elmer Digital Data Recorder). The digital output was recorded on paper punch tape (Iomec Inc.). The range of the digital output is from 0 to 10 000 units, which corresponds to full-scale displacement of the DSC recorder. Heat capacity data points were sampled every 1.2 s.

The heat capacity calculations from the recorded amplitudes were performed on a Hewlett-Packard 9821A programmable calculator. The DSC output on tape was read by an optical tape reader (HP2748B) and assimilated into the calculator. The details of the program used in the evaluation of the heat capacity have been discussed earlier $[5]$.

Benzoic acid (Baker, reagent grade) was used as the calibration standard over the temperature range 100-260 K. Sapphire (Perkin-Elmer 219-036) was used as the standard in the temperature range 210-620 K. The temperature scale was calibrated using various standards as described earlier $[6]$. The accuracy of the measured temperature is estimated to be ± 0.2 K. The accuracy of the heat capacity measurements is estimated to be $\pm 2\%$ in the temperature range 100-300 K [7] and better than $\pm 1\%$ from 300 to 620 K [5].

Sample preparation and pan loading procedures

Tin sesquisulfide, $Sn₂S₃$, was prepared by annealing stoichiometric amounts of tin (99.999%) and sulfur (99.999%) in previously cleaned [8] and evacuated ampoules of fused silica at about 770 K for 300 h. During the above annealing period, the material was removed from the ampoule and ground repeatedly to ensure complete reaction. The crystallographic identity of the material was established by X-ray diffraction techniques. All reflections of Debye-Scherrer powder photographs (114.59 mm diameter camera, Ni-filtered CuK α radiation) could be indexed on the basis of an orthorhombic unit cell. The calculated lattice parameters $(a_0 = 0.8771 \pm 0.0017 \text{ nm}$, $b_0 = 0.3742 \pm 0.0007$ nm, $c_0 = 1.403 \pm 0.003$ nm) were in good agreement with literature values [9-11]. Prior to loading the samples into the aluminum pans, the material was outgassed at about 375 K for 2 h at a pressure of about 10^{-4} Pa.

For the heat capacity measurements, all samples were loaded and sealed in aluminum pans in a dry box containing a desiccated nitrogen atmosphere. Hermetically sealed pans were used in the heat capacity measurements from 220 to 610 K. Non-hermetically sealed pans were used in the low temperature measurements (110-260 K) to accommodate larger amounts of samples. The low temperature heat capacity measurements did not require hermetic sealing of the pans since reactions of the sample under these temperature conditions are unlikely. The mass of the powdered sample was determined by weighing the pan and cover before and after loading using a Cahn microbalance with an accuracy of ± 0.02 mg. The pans were filled with sample and sealed to minimize the free volume containing nitrogen_ **At the** end of each heat capacity run, the sample plus pan were weighed to confirm constant mass. In all cases the mass of the sample plus pan remained constant within ± 0.02 mg for total weights of about 60 mg. Microscopic examination of the opened pans revealed no visible reaction between the samples **and the aluminum containers.**

Heat capacity measurements

In the first run, the heat capacity of Sn₂S₃ was measured in the temperature range $100-260$ K using a sample mass of 53.62 mg. The heat capacity **data were obtained in temperature intervals of 40 K using a heating rate of** 20 K min⁻¹ with a sensitivity of 21 mJ s⁻¹. The sample was then cooled to 100 K and the heat **capacity measurement was repeated.**

In the second and third runs, $Sn₂S₃$ samples of masses 40.11 and 39.22 **mg, respectively, were used. Heat capacity measurements for each of these samples were recorded from 220 to 610 K at a heating rate of** 10 **K min-'** and a sensitivity of 21 mJ s⁻¹ in temperature intervals of 40-70 K. After **completion of a run for a given sample, the sample was cooled to** 210 K and the heat capacity measurement was repeated.

RESULTS

The results of the heat capacity measurements on Sn₂S₃ in the tempera**ture range 110-610 K are represented graphically in Fig. 1. (Because of the overlap of experimental data obtained from the individual runs, only part of the 184 individual heat capacity data appears in Fig. 1.) The determination** of the heat capacity of $Sn₂S₃$ was terminated at or near 610 K. Above 610 K thermal effects attributable to the thermal decomposition of $Sn₂S₃$ were **observed [lb]** _

A **least-squares treatment of all the** heat capacity data yields the equation

 $\ln C_p^0 = 0.0991872(\ln T)^3 - 1.85497(\ln T)^2 + 11.6663 \ln T$

 $-19.8237(J K^{-1} mole^{-1})$

which is valid over the temperature range 110-610 K. The standard devia-

Fig. 1. The heat capacity of $Sn₂S₃$ as a function of temperature. (^a) selected measured **heat capacity data;** (0) **extrapolation of the heat capacity to absolute zero.**

(1)

tion of experimental heat capacity data from eqn. (1) is ± 0.78 J K⁻¹ mole⁻¹ with a root-mean-square deviation of $\pm 0.7\%$ for all data.

DISCUSSION

The calculation of the thermodynamic parameters $H_T^0 - H_0^0$, S_T^0 and G_T^0 - H_0^0 from measured heat capacity data requires a knowledge of the heat capacity to temperatures close to absolute zero. Unfortunately, instrument limitations prevented measurements below 100 K. Because of the anisotropic structure of $Sn₂S₃$ as discussed below, a representation of the measured heat capacity data based on the Debye equation [12]

$$
\frac{C_{\rm v}}{15\ R} = D\left(\frac{\theta_D}{T}\right) \tag{2}
$$

for the temperatures of this study is not expected to be satisfactory.

The low and high temperature heat capacities of SnS and SnS_2 have been investigated earlier [3,4]. A structural comparison of the tin sulfides SnS, $Sn₂S₃$ and $SnS₂$ suggested bonding similarities in these compounds [11]. This would allow an extension of Kopp's rule [13] to yield the low temperature $(0-100 \text{ K})$ heat capacity of Sn_2S_3 as the sum of the heat capacities of SnS and SnS $(3,4]$.

 $Sn₂$ crystallizes in an orthorhombic structure [9–11] with di- and tetravalent Sn atoms [10,111. The average length of the $Sn(IV)$ —S bonds in $Sn₂S₃$ is about 0.256 nm and nearly equals that of the $Sn(IV)-S$ bonds (0.258 nm) in SnS₂ [14]. The average Sn(II)-S bond length in $Sn₂S₃$ is 0.268 nm, which closely approximates the average of the shorter $Sn(II)-S$ bonds (0.266 nm) in SnS $[15]$. The structure of SnS is orthorhombic $[15]$ with the same space group as that of $Sn₂S₃$ [10,11]. Similarities between the hexagonal [14] structure of $SnS₂$ and the structure of $Sn₂S₃$ have been reviewed earlier [11]. These similarities show that the tin-sulfur bonds in $Sn₂S₃$ closely resemble the corresponding bonds in SnS and SnS.

In order to demonstrate that the measured heat capacity of $Sn₂S₃$ in the range 110-610 K approsimates the sum of the heat capacities of SnS and $SnS₂$, a re-evaluation of the earlier data [3,4] for the temperature range of the present study was required.

The heat capacity of SnS

The low temperature heat capacity of SnS has been measured in the temperature range $52.45-298.15 K [3]$, and the results were empirically fitted [3] to the equation

$$
\frac{C_{\rm p}^{\rm o}}{3\,R} = D\left(\frac{146}{T}\right) + E\left(\frac{311}{T}\right) \tag{51-150 K}
$$

The quantity $D(146/T)$ represents the Debye function [12] with a θ -temperature of 146 K. The term $E(311/T)$ is the Einstein function [16] with a θ temperature of 311 K.

TABLE 1 Calculated thermodynamic parameters for SnS(s)^a

^a The number of figures reported in columns 2, 3, 4 and 5 has only calculational significance.

The high-temperature heat capacity of SnS was later determined from 298.15 to 1225 K [4]. A phase transformation of SnS at 875 K reported earlier [4] was recently identified as a transition from a distorted NaCl to the orthorhombic TlI-type structure [17,181.

To facilitate a direct comparison of the heat capacity of SnS with that of Sn₂S₃, the heat capacity of SnS was computed or interpolated at rounded temperatures in increments of **lo-50 K. The results are shown in Table 1.** In addition, the thermodynamic parameters $H_T^0 - H_0^0$, S_T^0 and $-(G_T^0 - H_0^0)$ **were calculated from the heat capacity of SnS in Table 1 and are listed in columns 3, 4 and 5, respectively.**

The heat capacity function of SnS

$$
\ln C_{\rm p}^{0} = 0.114905(\ln T)^{3} - 1.99273(\ln T)^{2} + 11.6659 \ln T
$$

- 19.1440(J K⁻¹ mole⁻¹) (4)

was obtained from a least-squares analysis of the data of SnS in the temperature range loo-875 K. The standard deviation of the esperimental heat capacity data [3,4] from eqn. (4) is ± 0.24 J K⁻¹ mole⁻¹ with a root-meansquare deviation of $\pm 0.5\%$.

The heat capacity of SnS-,

The low-temperature heat capacity of Sr& was measured from 52.75 to 298.15 K [3]. The data were empirically fitted [3] to the equation

$$
\frac{C_p^0}{3 R} = D\left(\frac{172}{T}\right) + E\left(\frac{369}{T}\right) + E\left(\frac{415}{T}\right) \qquad (51-170 \text{ K})
$$
 (5)

The quantities $D(172/T)$ with a 0-temperature of 172 K, $E(369/T)$ and $E(415/T)$ with θ -temperatures of 369 and 415 K, respectively, represent the **Debye [121 and Einstein functions [161.**

The high-temperature heat capacity of SnS₂ was later measured from **298.15 to 1005 K [4]. To facilitate a direct comparison of the earlier heat** capacity measurements on SnS₂ [3,4] with that of Sn₂S₃, the heat capacity of SnS₂ was computed or interpolated at rounded temperatures in incre**ments of lo-50 K.**

The results are shown in Table 2. The thermodynamic quantities H_T^0 – H_0^0 , S_T^0 and $-(G_T^0 - H_0^0)$ were computed from the heat capacity data of SnS₂ **in Table 2 and are listed in columns 3, 4 and 5, respectively.**

A least-squares treatment of the heat capacity data of SnS, of earlier authors [3,4] in the temperature range 100-1005 K yielded the relationship

$$
\ln C_{\rm p}^{0} = 0.112224(\ln T)^{3} - 2.10132(\ln T)^{2} + 13.2230 \ln T - 23.6488(J K^{-1} \text{ mole}^{-1})
$$
\n(6)

The standard deviation of the heat capacity data [3,4] from eqn. (6) is ± 0.38 J K⁻¹ mole⁻¹ with a root-mean-square deviation of $\pm 0.7\%$.

192

a The number of figures reported in columns 2, 3, 4 and 5 has only calculational significance.

Thermodynamic properties of SnzS3

Table 3 shows the thermodynamic data for $Sn₂S₃$. A comparison of the heat capacity of $Sn₂S₃$ computed in the temperature range 100-650 K from eqn. (1) with the sum of the heat capacities of SnS (Table 1) and SnS₂ **(Table 2) shows close correspondence. The relationship**

$$
C_p^0(\text{Sn}_2\text{S}_3) = C_p^0(\text{SnS}) + C_p^0(\text{SnS}_2)
$$
\n(7)

is accurate within $\pm 2\%$. Based on the bonding and structural similarities of **these compounds discussed above, this result is expected.**

Because of the close agreement of the heat capacity of $Sn₂S₃$ based on eqn. (1) with the results of eqn. (7) in the temperature range 100–650 K, we propose that the low-temperature heat capacity of $Sn₂S₃$ can similarly be **estimated at lower temperatures by the sum of the heat capacities of SnS** and SnS₂. The results of the calculations are entered in Table 3 for the tem**perature range O-100 K.**

From the heat capacity data of Sn₂S₃ (Table 3), the thermodynamic quantities $H_T^0 - H_0^0$, S_T^0 and $-(G_T^0 - H_0^0)$ were calculated at various temperatures **and are listed in columns 3, 4 and 5, respectively.**

The absolute entropy, enthalpy and free enthalpy of *Sn2S3* **were thus** determined to be $S_{298}^0 = 163.6 \pm 6$ J K⁻¹ mole⁻¹, $H_{298}^0 - H_0^0 = 23.7 \pm 1$ kJ mole⁻¹ and $G_{298}^0 - H_0^0 = -25.1 \pm 2 \text{ kJ}$ mole⁻¹, respectively. The absolute entropy of Sn₂S₃ based on heat capacity measurements compares favorably with the entropy value $(170.5 \pm 6 \text{ J K}^{-1} \text{ mole}^{-1})$ determined from Knudsen **effusion studies [lb].**

Kelley has tabulated entropy constants for elements which, when added appropriately yield the absolute entropy of compounds [19]. Using these entropy data [19], the absolute entropy of $Sn₂S₃$ is calculated to be $S₂₉₈⁰$ = 160.2 ± 8 J K⁻¹ mole⁻¹.

SUMMARY AND CONCLUSIONS

The heat capacity of $Sn₂S₃$ was determined in the temperature range 110– 610 K. Extrapolation of the heat capacity of Sn₂S₃ from 110 to 0 K was **done by summing r;he empirical heat capacity equations of SnS and Sn&** [3]. The addition of the heat capacities of SnS and SnS₂ to yield that of Sn₂S₃ is based on structural and bonding similarities between these com**pounds.**

The thermodynamic quantities $H_T^0 - H_0^0$, S_T^0 and $-(G_T^0 - H_0^0)$ were calculated from 0 to 650 K. The absolute entropy of $Sn₂S₃$ at 298 K is 163.6 \pm 6 **J K-l mole-'. This value agrees favorably with the absolute entropy obtained** from Knudsen effusion studies (S^y₂₉₈ = Kelley's entropy constants [19] (S₂₉₈ = **170.5 J K-i mole-') [lb] and from 160.2 J K-i mole-'). Recent studies** on the heat capacities of I-III-VI₂ compounds revealed similar additive rela**tionships for these materials [201.**

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Calculated thermodynamic parameters for $Sn_2S_3(s)$ ^a

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^a The number of figures reported in columns 2, 3, 4 and 5 has only calculational significance.

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